

## Translation

This is the act of moving an object from one position to the next without turning. With a plane figure each point moves the same distance and in the same direction. All points undergo the same displacement.

## Image under a translation

When the (object) point  $G(x, y)$  undergoes a translation or displacement  $T = \begin{pmatrix} x' \\ y' \end{pmatrix}$  then it is mapped onto  $G'(x', y') = G'(x + x', y + y')$

## Translations as column vectors or matrices

$$\begin{matrix} G \\ \begin{pmatrix} x \\ y \end{pmatrix} \end{matrix} \quad + \quad \begin{matrix} T \\ \begin{pmatrix} x' \\ y' \end{pmatrix} \end{matrix} \quad = \quad \begin{matrix} G' \\ \begin{pmatrix} x + x' \\ y + y' \end{pmatrix} \end{matrix}$$

$$\begin{matrix} \text{Object} \\ \text{matrix} \end{matrix} \quad + \quad \begin{matrix} \text{Translation} \\ \text{matrix} \end{matrix} \quad = \quad \begin{matrix} \text{Image} \\ \text{matrix} \end{matrix}$$

## And

$$\begin{matrix} T \\ \begin{pmatrix} x' \\ y' \end{pmatrix} \end{matrix} \quad = \quad \begin{matrix} G' \\ \begin{pmatrix} x + x' \\ y + y' \end{pmatrix} \end{matrix} \quad - \quad \begin{matrix} G \\ \begin{pmatrix} x \\ y \end{pmatrix} \end{matrix}$$
$$\begin{matrix} \text{Translation} \\ \text{matrix} \end{matrix} \quad = \quad \begin{matrix} \text{Image} \\ \text{matrix} \end{matrix} \quad - \quad \begin{matrix} \text{Object} \\ \text{matrix} \end{matrix}$$

**Also**

<b>G</b>		<b>G'</b>		<b>T</b>
$\begin{pmatrix} x \\ y \end{pmatrix}$	=	$\begin{pmatrix} x + x, \\ y + y, \end{pmatrix}$	–	$\begin{pmatrix} x, \\ y, \end{pmatrix}$
Object	=	Image	–	Translation
matrix		matrix		matrix